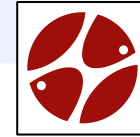




# Dielectric and Shear-Mechanical Dynamic Heterogeneities in Supercooled Liquids

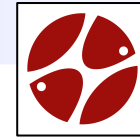
C. Maggi ([cmaggi@ruc.dk](mailto:cmaggi@ruc.dk))

DNRFF Centre 'Glass and Time', IMFUFA, Department of Sciences,  
Roskilde University, Postbox 260, DK-4000 Roskilde, Denmark



# Outline

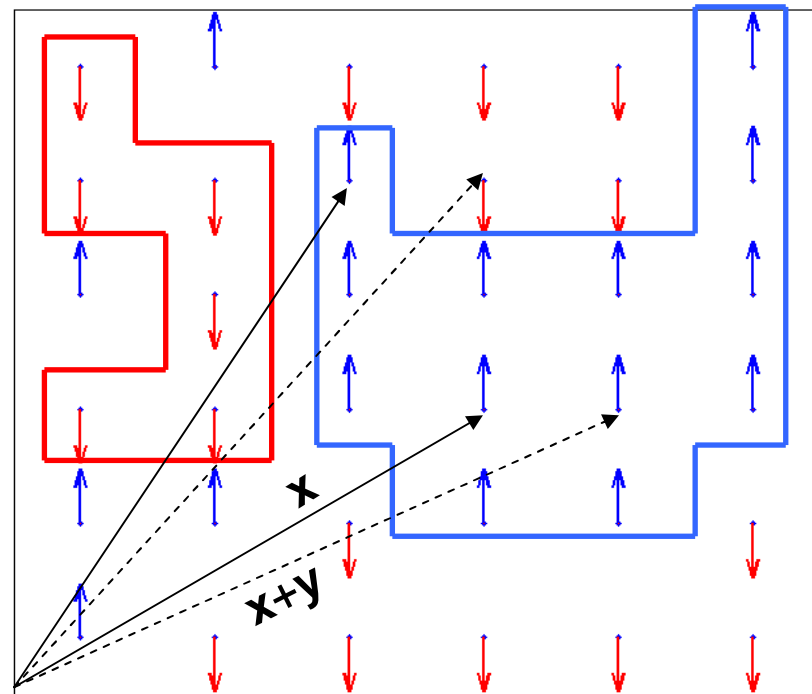
- Heterogeneities and four-point correlations
- Dielectric and shear-mechanical dynamic heterogeneity
- The case of a mono-alcohol with an additional dielectric relaxation
- Conclusions

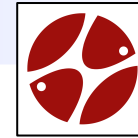


# The study of heterogeneities is inspired by *spin-glasses*<sup>[1]</sup>

- The spin-spin correlation is zero when averaged over space:  $[\langle s_x s_{x+y} \rangle]_x = 0$
- Introduction of the E.A. parameter:  $[\langle s_x s_{x+y} \rangle^2]_x \neq 0$
- Dynamic generalization of the E.A. param. to study the dynamics above  $T_c$ :

$$[\langle s_x(0)s_{x+y}(0)s_x(t)s_{x+y}(t) \rangle]_x \xrightarrow{t \rightarrow \infty} [\langle s_x s_{x+y} \rangle^2]_x$$





# Dynamic heterogeneity and its lower bound from the FDT<sup>[2]</sup>

- Generalization for any variable of a supercooled liquid:

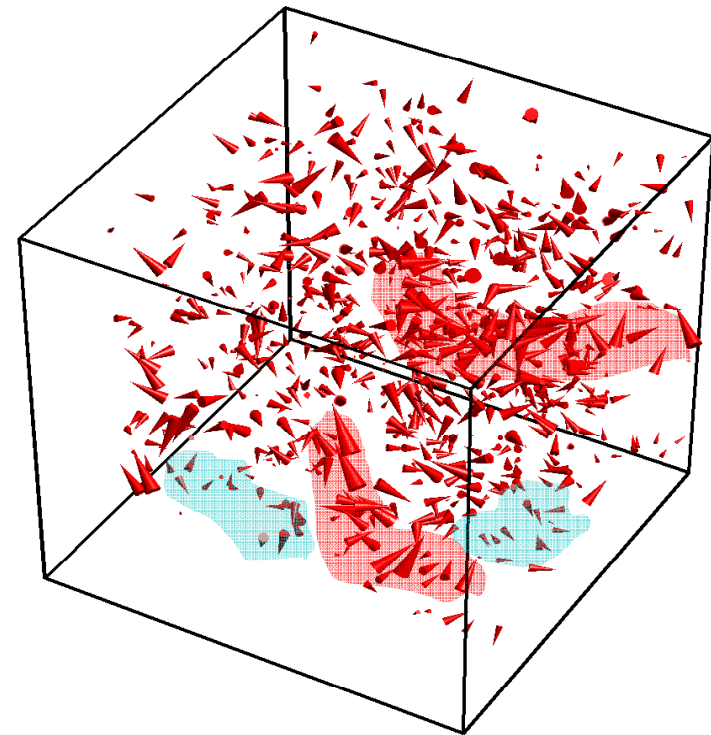
$$\frac{1}{N} \chi_4(t) = [[\langle \mathcal{O}_x(0) \mathcal{O}_x(t) \mathcal{O}_{x+y}(0) \mathcal{O}_{x+y}(t) \rangle]_x]_y - [\langle \mathcal{O}_x(0) \mathcal{O}_x(t) \rangle]_x^2$$

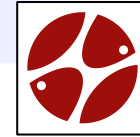
- Three point correlation and the Schwartz inequality:

$$\frac{1}{N} \chi_T(t) = [[\langle h_x(0) \mathcal{O}_{x+y}(0) \mathcal{O}_{x+y}(t) \rangle]_x]_y$$

$$[\frac{1}{N} \chi_T(t)]^2 \leq \frac{1}{N} \chi_4(t) \times [[\langle h_x(0) h_y(0) \rangle]_x]_y$$

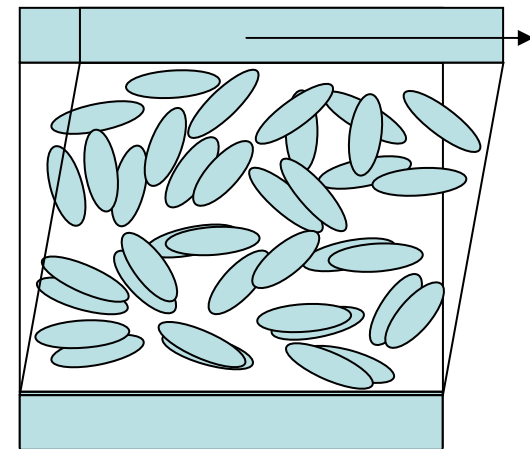
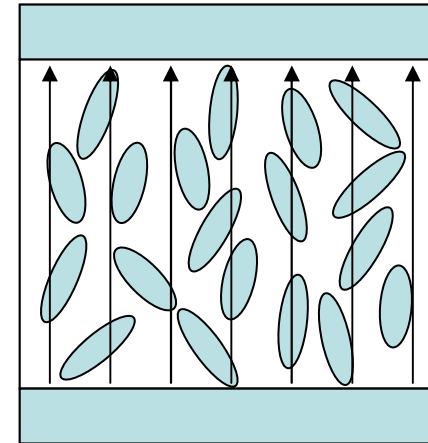
- **FDT**  $\chi_4(t) \approx \frac{T^2 \chi_T^2(t)}{c_P} = \frac{1}{c_P} \left( \frac{\partial C(t, T)}{\partial \ln T} \right)^2$





# Dielectric and shear-mechanical linear response

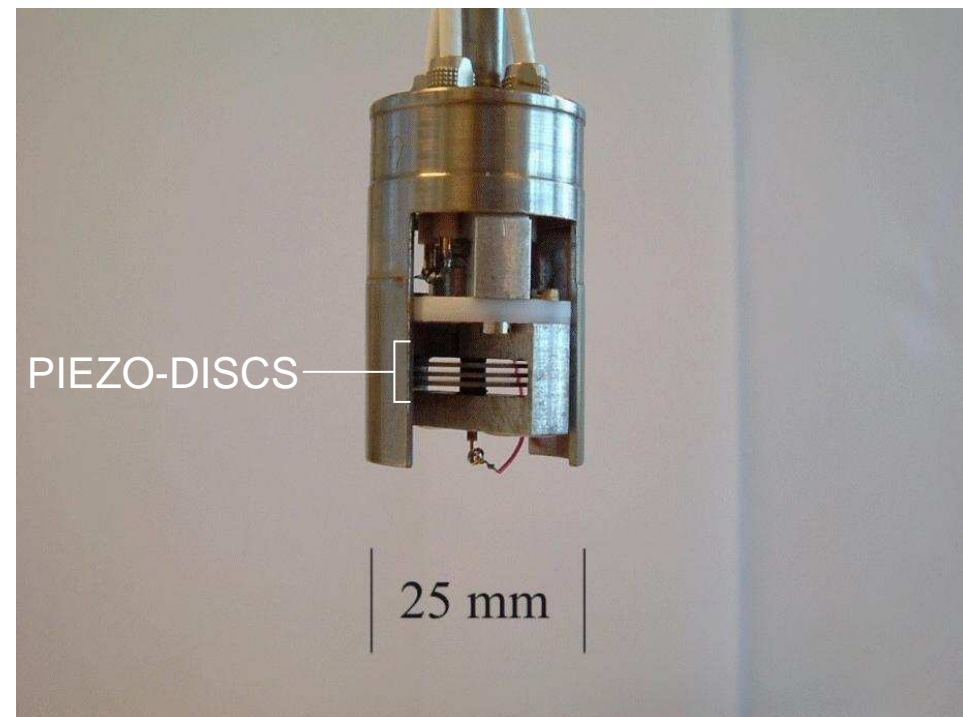
- The dielectric response is related to the dynamics of molecular dipoles
- The shear-modulus represents the resistance that the system opposes to a volume-preserving deformation



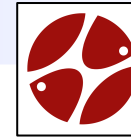


# Broad-band mechanical spectroscopy: the PSG technique<sup>[3]</sup>

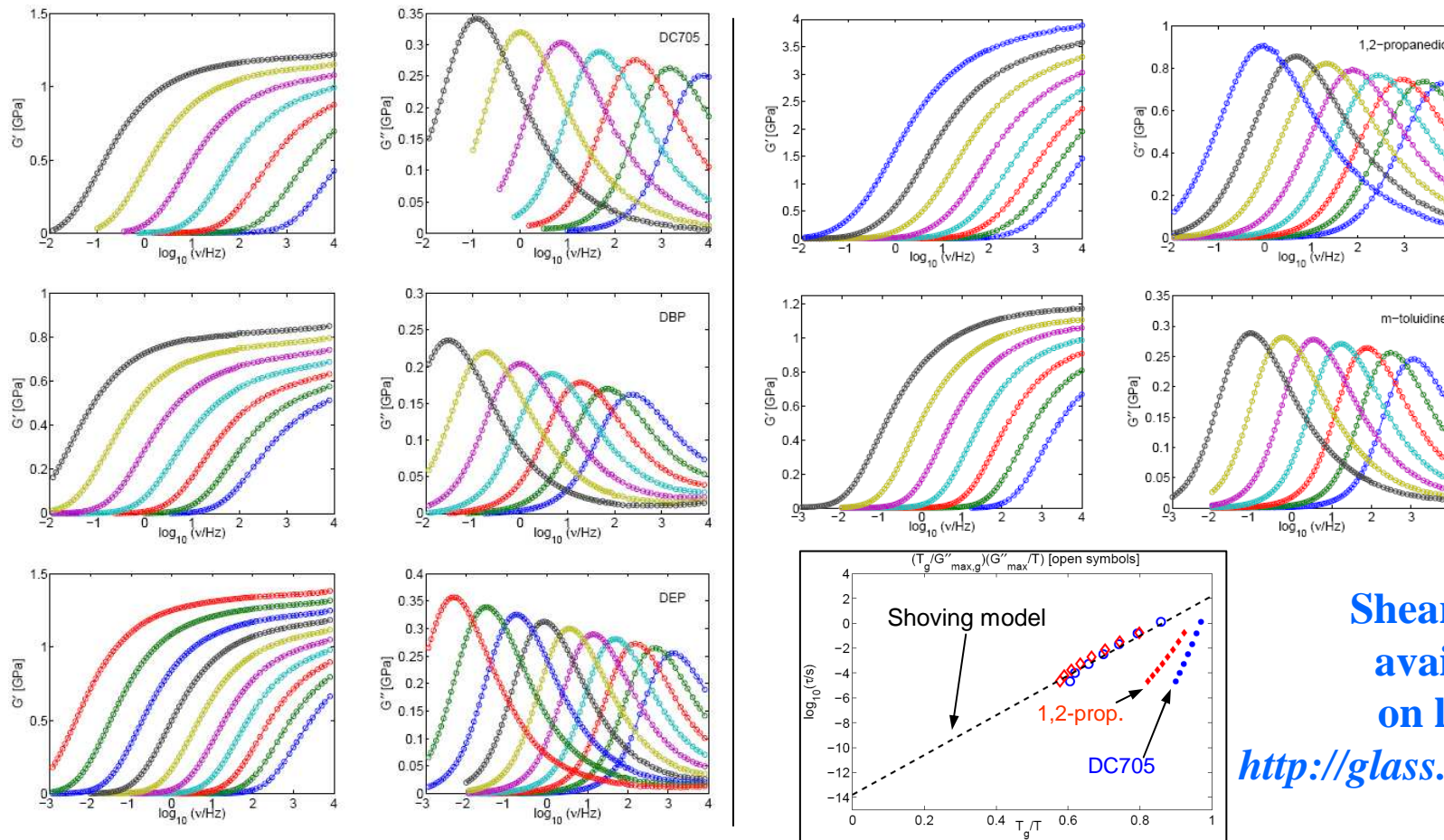
- The Piezoelectric Shear Gauge is composed by three piezoelectric discs
- These discs expand-contract under the action of the applied electric field
- The discs capacitance is determined by the shear-modulus of the liquid adhering to them.



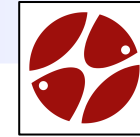
[3] T. Christensen and N. B. Olsen, *Rev. Sci. Instrum.* **66**, 5019 (1995).



# Broad-band mechanical spectroscopy: many informations on super-cooled liquids<sup>[4]</sup>



Shear-data  
available  
on line at  
<http://glass.ruc.dk/data> !



## Extraction of the dynamic heterogeneity<sup>[5]</sup>

- The response function needs to be normalized

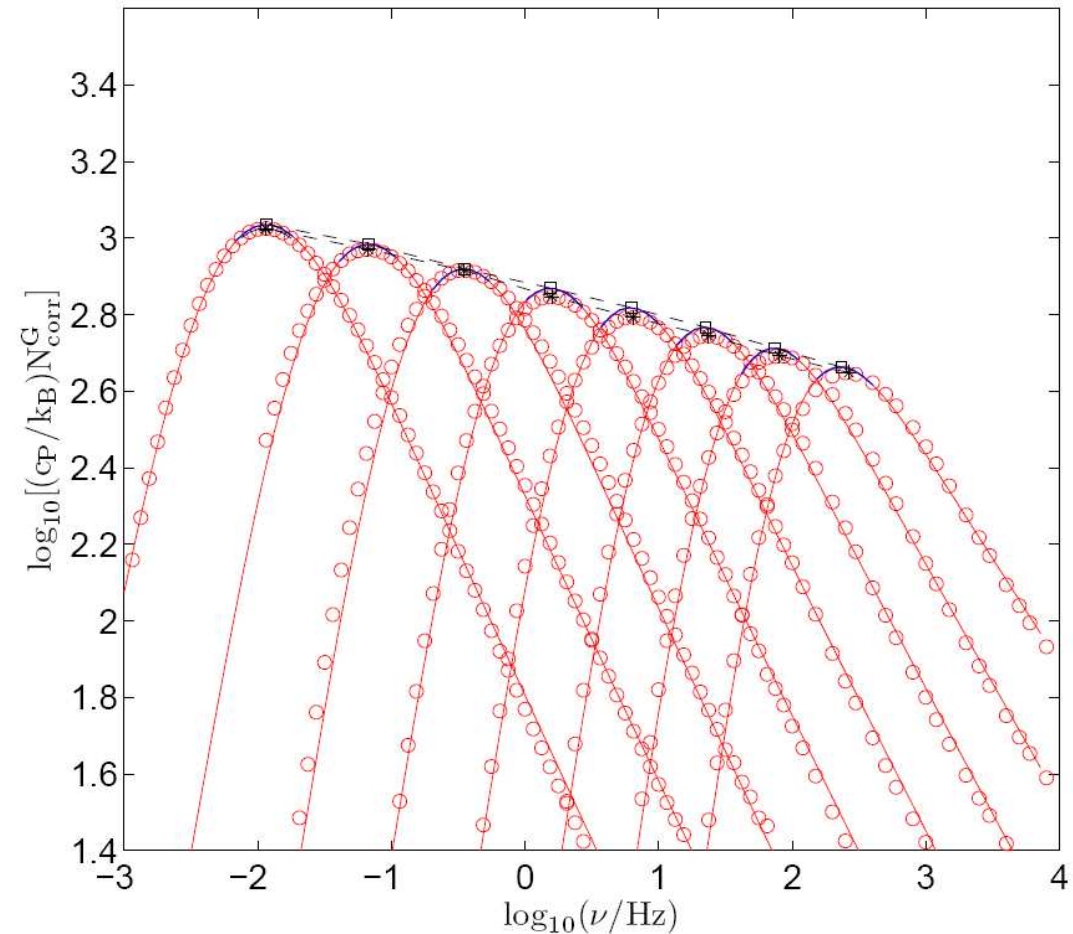
$$\chi_4(\omega) = \frac{1}{c_P} \left( \frac{\partial \tilde{\chi}(\omega, T)}{\partial \ln T} \right)^2$$

- The parameters are obtained fitting with the HN function

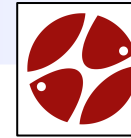
$$\chi(\omega) = \chi_\infty + \Delta\chi / [1 + (i\omega\tau)^\alpha]^\beta$$

- The *characteristic* dynamic heterogeneity is found

$$N_{corr} \simeq \max_{\omega} \left\{ \frac{1}{c_P} \left( \frac{\partial \tilde{\chi}(\omega, T)}{\partial \ln T} \right)^2 \right\}$$

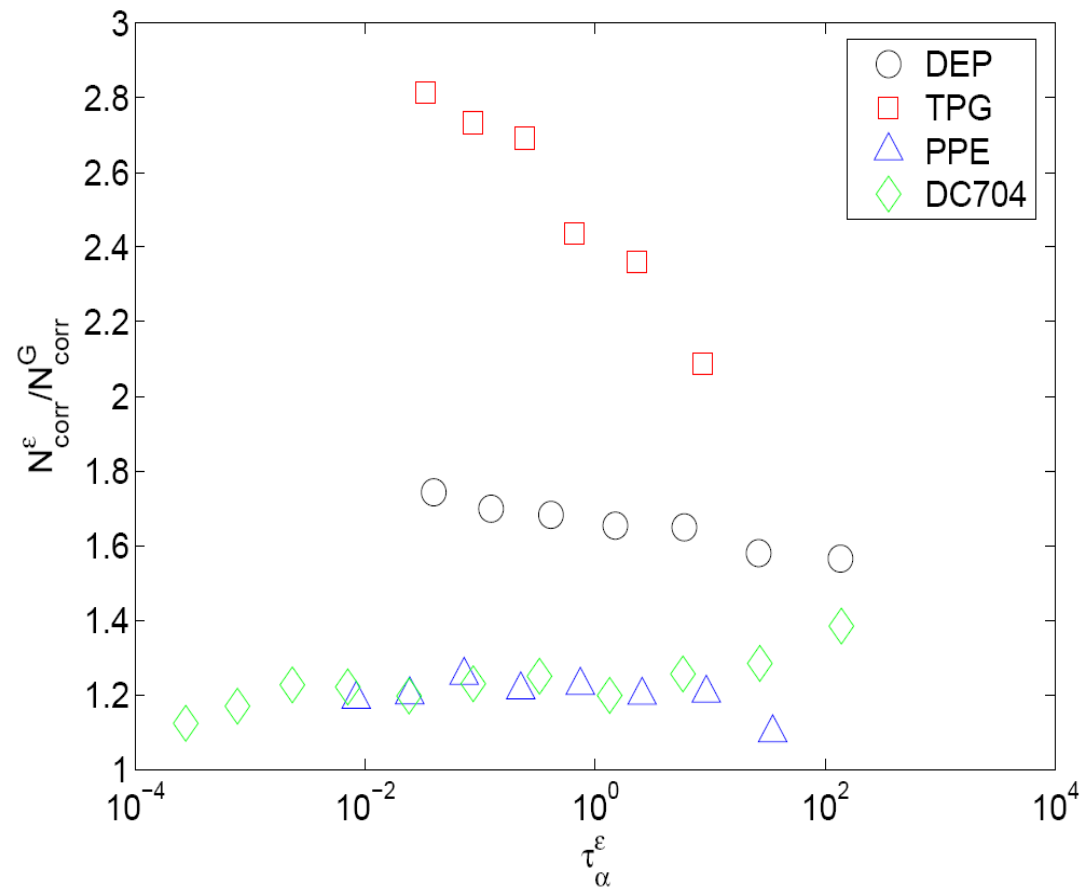


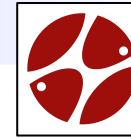




# Comparison of the heterogeneities<sup>[6]</sup>

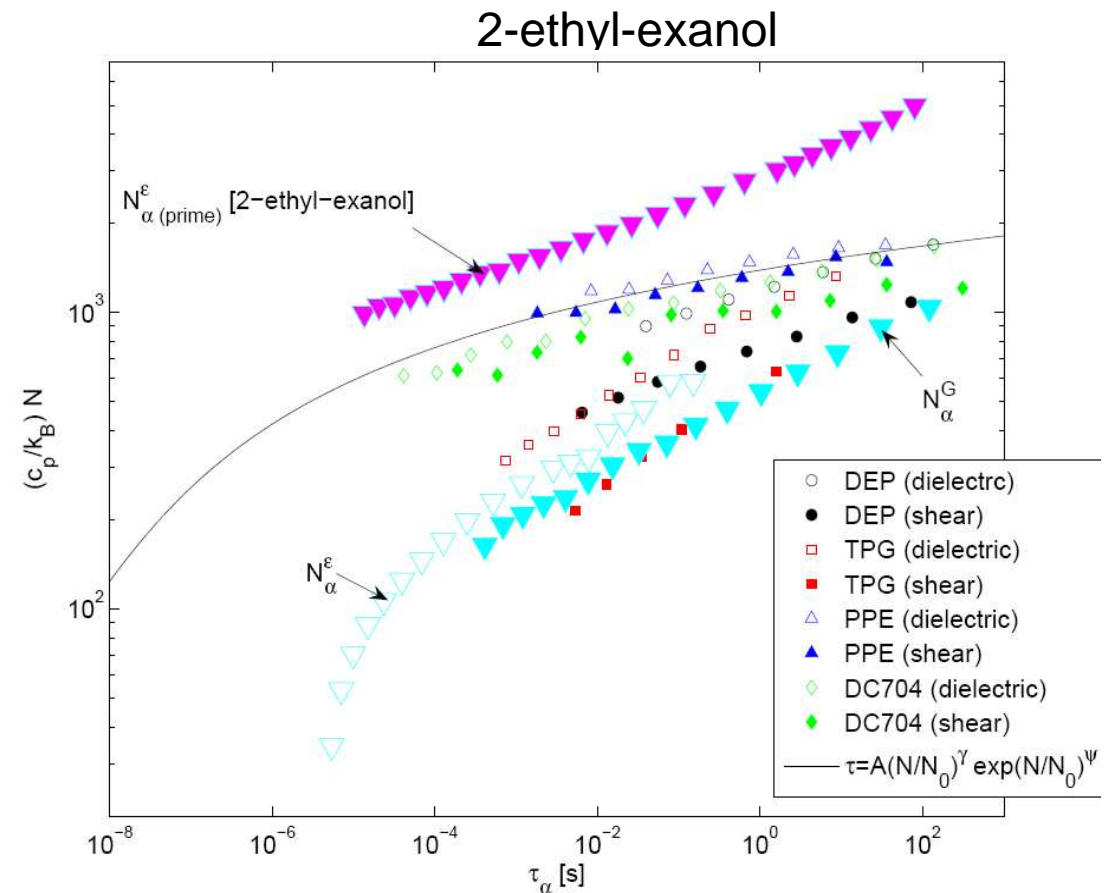
- The heterogeneity increases as temperature decreases
- The heterogeneity increases following the relaxation time
- The dielectric heterogeneity it is *always greater* than the shear-mechanical one



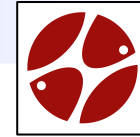


# The case of a mono-alcohol with an additional relaxation process<sup>[7]</sup>

- Some mono-alcohols show an additional (very intense) Debye-like dielectric relaxation process
- This process has not been detected in calorimetric measurements and density fluctuations
- We do not find this additional process in the shear-mechanical dynamics
- The behavior and the value of the heterogeneity of the different processes help us in classification



[7] B. Jakobsen, C. Maggi. et al. arXiv:0805.4519v2.



# Conclusions

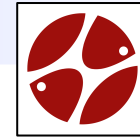
- **Our analysis shows that:**
  - 1) The dynamic correlation volume of the dielectric dynamics is *systematically larger* than the correlation volume of the shear-mechanical dynamics
  - 2) The study of the heterogeneity clearly distinguishes between multiple processes as in the case of mono-alcohols with additional dielectric processes (alpha prime).

## Acknowledgements:

*Glass and Time*

C. Dalle-Ferrier

C. Alba-Simionesco



*Thank you for your attention!*