Density scaling of structure and dynamics of an ionic liquid†

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Room temperature ionic liquids are salts with low melting points achieved by employing bulky and asymmetrical ions. The molecular design leads to apolar and polar parts as well as the presence of competing Coulomb and van der Waals interactions giving rise to nano-scale structure, e.g. charge ordering. In this paper we address the question of how these nano-scale structures influence transport properties and dynamics on different timescales. We apply pressure and temperature as control parameters and investigate the structure factor, charge transport, microscopic alpha relaxation and phonon dynamics in the phase diagram of an ionic liquid. Including viscosity and self diffusion data from literature we find that all the dynamic and transport variables studied follow the same density scaling, i.e. they all depend on the scaling variable $\Gamma = \rho^2/\gamma T$, with $\gamma = 2.8$. The molecular nearest neighbor structure is found to follow a density scaling identical to that of the dynamics, while this is not the case for the charge ordering, indicating that the charge ordering has little influence on the investigated dynamics.

1 Introduction

The main dynamical process of a liquid is the alpha relaxation, which is associated with the molecular mobility and thus usually directly related to transport properties such as the shear viscosity or ionic conductivity if ions are present. The alpha relaxation time and the viscosity both increase as the liquid is cooled down and when it is brought into the supercooled state the relaxation time and viscosity increase dramatically. This finally leads to the glass transition when the viscosity reaches $10^{12}$ Pa s and the alpha relaxation time is approximately 100 s.1,3 Applying pressure to a liquid provides an alternative route to slow down the dynamics. The temperature-pressure phase diagram of a liquid therefore contains lines, so-called isochores, along which the alpha relaxation time is constant. The glass-transition line, $T_g(P)$, is an example of an isochrone where the alpha relaxation is on the scale of minutes, but isochores exist also for the low viscosity liquid with relaxation times in the pico- to nano-second range. Likewise isolines in the phase diagram can be envisaged for transport properties, although they do not a priori coincide with the isochores. It has previously been shown that a density scaling of the viscosity or the relaxation time as a function of temperature and pressure applies for many molecular liquids and polymers, i.e. pressure and temperature behavior can be brought to collapse when expressed in terms of the parameter $\Gamma = \rho^2/\gamma T$, where $\gamma$ is a material specific constant and $\rho$ is the density.3–6 If different transport and dynamical variables obey density scaling with identical value of $\gamma$, then they also have identical isolines in the phase diagram.

In ionic liquids the conductivity, $\sigma$, is a key transport property. Conductivity decreases rapidly with decreasing temperature or increasing pressure and isoconductivity lines can readily be identified in the $(T,P)$ phase diagram. In contrast to simple liquids, ionic liquids are structurally ordered on the nanometer scale due to the competition between Coulomb and van der Waals interactions.7 Despite this structuring, density scaling in ionic liquids has been shown to hold for both viscosity,8–11 conductivity11–16 and self diffusion.11 Yet, density scaling has not been demonstrated before for the alpha relaxation in ionic liquids. Dielectric spectroscopy is the main technique for probing the alpha relaxation in non-conducting liquids, especially when it comes to high pressure studies. This technique, though, is not applicable for ionic liquids because the contribution to the dielectric signal from the conductivity overshadows the contribution of the alpha relaxation. However, the alpha relaxation can be accessed in the low viscosity liquid by quasi-elastic neutron spectroscopy (QENS).

In this work we investigate the pressure and temperature dependence of structure and dynamics with respect to density...
scaling in ionic liquids. We have studied the ionic liquid Pyr14TFSI (1-butyl-1-methylpyrrolidinium bis(trifluoromethanesulfonyl)imide). The methyl group and butyl chain on the cation are deuterated in the sample used for neutron scattering in order to mask the dynamics of these side groups. The anion has little incoherent scattering, thus mainly the cation dynamics is observed in the neutron data.

2 Experiments

To follow alpha relaxation dynamics in \((T,P)\) space we measure conductivity spectra and QENS simultaneously on the back-scattering instrument IN16B at Institut Laue-Langevin (ILL) by use of the high-pressure cell developed for this type of experiment. In the neutron spectroscopy experiment the large incoherent scattering cross section of hydrogen gives access to the self-motion of a molecule by measuring directly the dynamic structure factor. By double Fourier transform in space incoherent scattering, thus mainly the cation dynamics is observed in the neutron data.

All data shown from IN16B and IN5 have been reduced in the standard way using LAMP in the standard way using DAWN software. All data shown from IN16B and IN5 have been reduced in the standard way using LAMP in the standard way using DAWN software. All data shown from IN16B and IN5 have been reduced in the standard way using DAWN software.

3 Results and analysis

3.1 Density scaling of dynamics

In Fig. 3 we show three \((T,P)\) isoconductivity state points and the corresponding QENS spectra from IN16B along with data.
Fig. 4(a) demonstrates density scaling of the alpha relaxation signal as probed by neutron scattering using elastic fixed window scans (EFWS) from IN16B\textsuperscript{23} summed over all momentum transfers ($Q$) for statistical reasons along five isotherms and two isobars (note that no change in scaling is observed with $Q$ as shown in Fig. S2, ESI\textsuperscript{†}). The scaling exponent is determined by visual inspection as the value that gives the best collapse of data. The conductivity, simultaneously measured using the combined neutron and dielectric cell, is shown in Fig. 4(b) along with ambient pressure conductivity, $\sigma$, from ref. 27–29. In addition Fig. 4(b) shows the conductivity relaxation time $\tau_\sigma$ (determined as described in ref. 14) measured in a separate experiment along four isobars. The conductivity relaxation time gives an alternative measure of charge transport, which is readily determined in the viscous liquid where conductivity is strongly frequency dependent. The data in Fig. 4 is shown in absolute units, while theoretical arguments suggest that reduced units should be used.\textsuperscript{30,31} We show the same data using reduced units in the ESI\textsuperscript{†} (Fig. S3), but there is little difference in the case of Pyr14TFSI, which has also been shown in ref. 11. The scaling exponent, $\gamma$, is in all cases determined by visual inspection. The uncertainty is approximately ±0.2 for the high temperature data but could be higher at low temperatures where density has been extrapolated. The density scaling has previously been reported in ref. 11 for two of the properties (diffusion and viscosity) and the exponent has been determined from the glass transition line in ref. 32. Both these earlier works find $\gamma = 3$ for Pyr14TFSI. We consider this to be consistent with our result within the estimated error bars, but we find $\gamma = 2.8$ gives a significantly better collapse of the EFWS data which are measured at high temperature where density is also measured, meaning that this is the range with highest certainty of the determined $\gamma$-value. In addition we also find that $\gamma = 2.8$ gives a better collapse for the diffusion data from ref. 27 which were used in ref. 11. The density scaling of these data is shown in Fig. 4(c) using $\gamma = 2.8$. We have shown all the density scaling figures in the ESI\textsuperscript{†} using $\gamma = 3$ (Fig. S4, ESI\textsuperscript{†}).

Fig. 4 From Fig. 4, it is clear that charge transport (conductivity and conductivity relaxation time), self diffusion, viscosity and the microscopic alpha relaxation all obey identical density scaling, i.e. a universal behavior is observed with the same exponent, $\gamma = 2.8$, for all quantities scaling with $I = \rho^2/T$. Identical density scaling does not imply that all properties behave in the same way. In fact, viscosity and diffusion have significantly different $I$-dependence in Fig. 4(c). However, identical density scaling does imply that the relative influence of density and temperature is the same for all properties. The consequence is that knowledge of the isolines in the phase diagram of one of these properties predicts the isolines of the others. In Table 4.2 of ref. 33 there is a compilation of the density scaling exponents from conductivity and viscosity for a number of different liquids. The exponents are very close, especially when considering ILs without hydrogen bonding, suggesting that this finding could be general.

The value of the scaling exponent, $\gamma = 2.8$, found from the density scaling of our data agrees well with previous observations for ionic liquids with $\gamma = 2–3$ reported in literature.\textsuperscript{8,10,16,34}
It is worth noting that this places ionic liquids at an intermediate level between the typical values for simple van der Waals liquids, where $g$ is often between 4 and 6, and hydrogen bonded liquids where $g$ typically is below 2 in the cases where density scaling holds for hydrogen bonding liquids.\textsuperscript{35–38}

### 3.2 Density scaling of structure

Considering the presence of nano-scale ordering\textsuperscript{17,18} in ionic liquids it is of interest to connect the changes in the dynamics to the evolution of the structure.

In Fig. 5 we show the structure factor at four state points. The peak observed around $Q \sim 0.8 \text{ Å}^{-1}$, is related to charge ordering, \textit{i.e.} the fact that the ions pack in a manner that insures charge neutrality on intermediate length scales\textsuperscript{7} whereas the peak at $Q \sim 1.2 \text{ Å}^{-1}$ is the molecular peak arising from nearest neighbor distances, typically found also in ordinary molecular liquids.\textsuperscript{39}

The inset of Fig. 5(a) illustrates the investigated state points chosen around an approximate isoconductivity line, such that the involved pressure and temperature changes have equivalent effect on the conductivity. In Fig. 5(a) the data are shown as measured, whereas in (b)–(d) the data are shown as a function of the reduced (dimensionless) wave vector $Q = Q \rho^{-1/3}$ to compensate for trivial density effects. Fig. 5(b) shows two isoconductivity state points, (c) shows two isothermal state points and (d) shows two isobaric state points. It is seen in Fig. 5 that the intensity of the charge ordering peak clearly depends on pressure, but only weakly depends on temperature. The intensity of the molecular peak, however, does not change dramatically with neither temperature nor with pressure. Yet, the collapse of the structure...
factors around the molecular peak of the two isoconductivity state points is better than along the isobar and the isotherm, obvious in particular in the minima between the two peaks.

To obtain a more quantitative comparison of the structure factors of the different state points we fit the peak positions of three isotherms measured from 0.1 to 400 MPa and plot them as a function of $\Gamma = \rho^3 / T$ (Fig. 6). This plot shows that the molecular peak positions collapse in a density scaling while the position of charge ordering peak does not (see also Fig. S5, ESI†). This shows that the molecular peak position is identical along the isolines of conductivity, viscosity and microscopic alpha relaxation. The observed density scaling of the molecular peak, but not of the charge ordering peak, indicates that the nearest neighbor order is directly connected to the dynamics, while the longer range charge order has a less direct effect on the dynamic variables.

3.3 Boson peak behavior

So far the analysis mainly focused on dynamics and structure in the low viscosity liquid phase, i.e. above the melting line. In the following we consider instead dynamics along the glass transition line. In a recent paper, Lima et al. show that the $T_g(P)$ line of Pyr14TFSI is also a line of constant $\Gamma = \rho^3 / T$, in the pressure range considered in our work. The exponent $\gamma = 3$ from that work is as discussed in Section 3.1 consistent with the value $\gamma = 2.8$ we find. From frequency dependent conductivity measurements we find that $T_g(P)$-line is also an isoline of the conductivity (Fig. S6, ESI†). The $T_g(P)$ line is by definition an isochrone of the macroscopic alpha relaxation and this is therefore another example of how different dynamic isolines collapse. Moreover, it shows that the $T_g(P)$-line can be determined from conductivity measurements consistent with studies showing how the conductivity of series of chemically similar systems can be scaled when plotted as $T/T_g$.29

Along the glass transition line $T_g(P)$, we have simultaneously with the frequency dependent conductivity measured QENS spectra of Pyr14TFSI on the time-of-flight instrument IN5 at the ILL.21 IN5 has a coarser energy resolution, in this case with an energy resolution of 0.1 meV providing a window into picosecond dynamics, i.e. faster than what was probed with IN16B. The alpha relaxation is on the scale of minutes at $T_g$ and therefore completely out of the experimental window of IN5. Instead the experiments probe vibrational dynamics, in particular, the excess in the density of states, a characteristic dynamical feature of glass-forming liquids, referred to as the Boson peak.40

Merged with the Boson peak is the fast relaxation which is seen as a broadening of the central peak. Fig. 7 shows the neutron spectra of Pyr14TFSI measured at the $T_g(P)$-line and in the glassy state with the spectrometer IN5. As for the IN16B experiment, we have used a sample with deuterated methyl and butyl chains, which means that the data is mostly sensitive to the dynamics of the carbon ring of the cation. Fig. 7 also shows equivalent spectra from a van der Waals liquid 5-polyphenyl ether (PPE) and a hydrogen bonded liquid dipropylene glycol (DPG) for comparison all plotted as a function of a reduced energy unit following work by some of us in ref. 19. Data are summed over $Q$, as there is no observable difference in behavior for the different values of $Q$ (Fig. S7 for Pyr14TFSI, ESI†).

For Pyr14TFSI, the Boson peak at $T_g$ is observed to be a shoulder merged with the fast relaxations, resembling the van der Waals liquid (PPE), contrary to the hydrogen bonded liquid (DPG), where an actual peak is observed. However, for the Boson peak in the glass, there is no obvious qualitative difference between the three materials. This suggests that the difference at $T_g$ stems from the fast relaxation, which is much more prominent in the van der Waals liquid and ionic liquid than in the hydrogen bonded liquid. The qualitative difference may relate to the proposed connection between fragility and
relative Boson peak intensity,\textsuperscript{41,42} and it puts the behavior of the ionic liquid in the category with fragile van der Waals liquids, consistent with the findings regarding fragility for similar ionic liquids in ref. 43.

It has previously been shown that the Boson peak and the fast relaxation are invariant along the $T_g(P)$-line, for van der Waals liquids, but not for hydrogen bonded liquids.\textsuperscript{19} Considering the spectra along the $T_g(P)$-line in more detail it is seen that they are not invariant for Pyr14TFSI. On the other hand, keeping in mind that the two state points on the $T_g(P)$-line have been determined just from having the same conductivity, a macroscopic long-time property, it is still a remarkable collapse of the microscopic dynamics including both fast relaxation and Boson peak.

4 Conclusion

Density scaling and the consequential collapse of different isolines hold exactly for model liquids governed by inverse power law pair potentials\textsuperscript{44} and can be explained in terms of isomorph theory.\textsuperscript{45} However, the competing van der Waals and Coulomb interactions and the different length scales in the structure of ionic liquids are at odds with these pictures, and in this case there is no \textit{a priori} reason to believe that density scaling should hold with the same scaling exponent for different dynamic variables. Yet we find density scaling and collapsing isolines of conductivity, microscopic alpha-relaxation, viscosity, self diffusion, macroscopic alpha-relaxation (\textit{i.e.} the $T_g(P)$-line) and to a large extend microscopic fast dynamics along $T_g(P)$ in the ionic liquid Pyr14TFSI. Thus, the behavior of the ionic liquid is similar to that of a van der Waals liquid, but there are also features that place the ionic liquid as an intermediate between van der Waals liquids and hydrogen bonded liquids: The value of the scaling exponent is intermediate ($\gamma = 2.8$ for Pyr14TFSI), and the imperfect collapse of the fast relaxation and Boson peak along the $T_g(P)$-line has reminiscence of the behavior seen for a hydrogen bonded liquid.

Recent simulations of a model ionic liquid have shown that the strength of the Coulomb interactions influence the alpha relaxation time,\textsuperscript{46} and it is also clear from the values of the scaling exponent $\gamma$ that the dynamics of ionic liquids are significantly different from van der Waals liquids. Given that Coulomb interactions are of higher energy than hydrogen bonds, it is nevertheless surprising to find the ionic liquids in an intermediate position – in fact leaning towards the van der Waals behavior. The molecular structure factor peak, scales with the same variable $\Gamma = \rho^*/T$, with exponent $\gamma = 2.8$, as the dynamics while the charge ordering peak does not obey this scaling. The molecular peak is a measure of nearest neighbor distance and it is the structural feature ionic liquids and van der Waals liquids have in common. Density scaling of the molecular peak therefore supports the picture that the van der Waals interactions and the short range order play the main role for the dynamics, while the Coulomb interactions and the charge ordering play a much less significant role. This picture could be different in ionic liquids where the cation is

Fig. 7 IN5 spectra on the glass transition isochrone showing the boson peak and fast relaxation. (a) For the ionic liquid Pyr14TFSI studied in this paper, (b) and (c) show data from ref. 19 for comparison. (b) The van der Waals liquid PPE and (c) the hydrogen-bonded DPG. All data are summed over $Q$ in constant $Q$-slices, $Q = 1.2$ to $1.8\,\text{Å}^{-1}$.
more bulky e.g. with longer alkyl-chains. In these liquids there is yet another level of ordering,\textsuperscript{17,18} which affects the dynamics at ambient pressure.\textsuperscript{17,18}

The conductivity and density data presented in this paper can be obtained from the “Glass and Time” data repository http://glass.ruc.dk/data/.

Conflicts of interest
There are no conflicts to declare.

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