



Toward broadband mechanical spectroscopy

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Diverse material classes exhibit qualitatively similar behavior when made viscous upon cooling toward the glass transition, suggesting a common theoretical basis. We used seven different measurement methods to determine the mechanical relaxation kinetics of a prototype molecular glass former over a temporal range of 13 decades and over a temperature range spanning liquid to glassy states. The data conform to time–temperature superposition for the main (alpha) process and to a scaling relation of schematic mode-coupling theory. The broadband mechanical measurements demonstrated have fundamental and practical applications in polymer science, geophysics, multifunctional materials, and other areas.

viscous liquids | broadband mechanical spectroscopy | mode-coupling theory

The extraordinary slowing down of viscous liquid dynamics upon cooling toward the glassy state plays a key role in myriad contexts, including polymer processing, survival of living organisms in extreme cold, amorphous metal synthesis, and many others. Glass-forming liquids display a number of common features, despite quite different chemistry ranging from high-temperature covalently bonded glass formers to van der Waals liquids that typically form glasses below room temperature (1–6). This commonality makes the research area attractive from a theoretical point of view and motivates the detailed study of selected liquid systems in the hope of revealing generic features of glass-forming liquids.

Viscoelastic relaxation behavior derives from two distinct and sequential processes common to all glass-forming liquids. The primary or “alpha” structural relaxation dynamics, which dictate the time scales for molecular diffusion and flow, are nonexponential in time, typically extend over several decades of time scales at a single temperature, and shift dramatically from picoseconds at high temperatures and low viscosities to many seconds as the sample is cooled and the glassy state is approached. This behavior gives rise to broad loss peaks in elastic compliance spectra, covering an extended frequency range at any temperature and shifting from gigahertz to millihertz frequencies as the temperature is lowered (Fig. 1). In addition to the temperature-dependent alpha relaxation dynamics, local rearrangements of molecules within existing cage geometries of the molecules, the so-called (fast) “beta” relaxation processes, result in a higher-frequency feature in the loss spectrum.

This scenario applies in the simplest cases when structural relaxation is slowed down through obstruction among neighboring molecules as in van der Waals liquids but not through extensive networks as in hydrogen-bonded liquids or entanglements as in polymers. In general, additional so-called Johari–Goldstein beta processes are observed (7, 8). For the present study, we chose a liquid with no such additional processes, to make the analysis as simple as possible.

A variety of semiempirical models (9–14), as well as the first-principles mode-coupling theory (MCT) (15, 16), have been developed in an effort to rationalize supercooled liquid dynamics. In its idealized “schematic” form, MCT predicts, for the local density dynamics, a critical temperature T_c at which there is a

transition from ergodic behavior above T_c to nonergodic behavior below, corresponding to arrest into a metastable glassy state.

A prominent feature in the last 50 years of discussions of viscous liquid dynamics is “time–temperature superposition” (TTS). TTS states that the alpha relaxation spectrum retains the same width and shape when the temperature is changed. A wide range of practices in polymer processing, rheology, aging, and other areas are based on TTS (17–21), but it has never been tested directly for mechanical properties across most of the time scales spanned. TTS forms the basis of many early heuristic descriptions of supercooled liquids extending from high temperature all of the way to the glass transition temperature; TTS is also predicted at $T > T_c$ by schematic MCT for the alpha process whenever it is well separated from the fast beta process (15, 16).

As input for theories of the dynamics of glass-forming liquids, information is needed over many decades of frequency (or time). Ideally, such broadband spectra should be taken for a large number of temperatures; this has been done spectacularly using dielectric relaxation spectroscopy, which covers an impressive 16 decades of frequency (22). Likewise, dynamic light scattering experiments cover 10 decades of frequencies (23). Unfortunately, neither technique monitors directly the density fluctuations, which, from a liquid-state theory viewpoint, are the most fundamental. Dielectric relaxation monitors the rotational degrees of freedom of polar molecules and molecular

Significance

Viscous liquids of all kinds, from honey to glycerol to common polymers, display remarkably similar dynamical properties upon cooling from high temperatures at which local structural relaxation and flow occur quickly, to moderate temperatures at which key components of the dynamics slow down dramatically, to cold temperatures at which a glassy solid is formed. The similarities suggest a common theoretical framework, but comprehensive measurements of liquids’ mechanical properties covering the extraordinary range of time scales spanned have been elusive. Using seven experimental methods covering 13 decades with few gaps, we demonstrate that broadband mechanical spectra are now within reach. Data obtained for the molecular glass former studied, a commercial silicone oil, follow key scaling laws predicted long ago.

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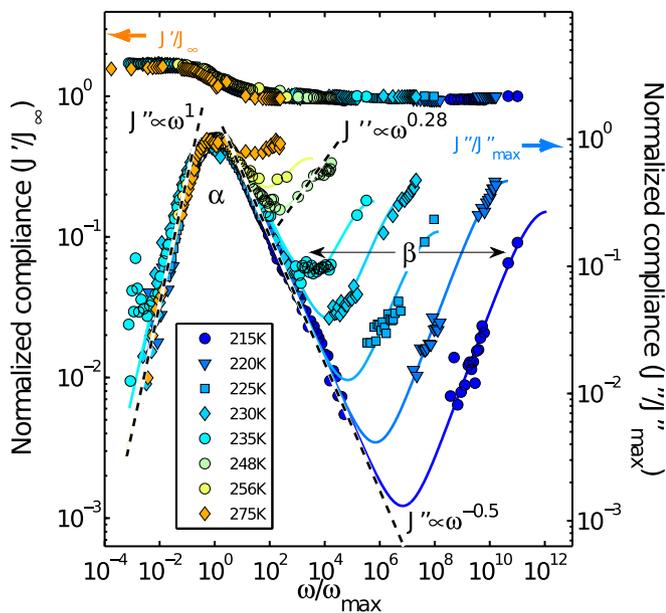


Fig. 3. Master plot of the compliance, demonstrating time-temperature superposition. The individual traces are scaled and shifted according to the fit values. The low-frequency side of the imaginary part follows a linear power law, $J'' \propto \omega^1$ (dashed line), corresponding to a simple exponential long-time decay of the stress autocorrelation function. The full curves give analytic model fits based on an alpha relaxation spectrum that follows an $\omega^{-0.5}$ high-frequency decay (compare *SI Appendix*, Fig. S18). The $\omega^{0.28}$ power law also shown here corresponds to the value found to fit the beta relaxation spectral wing near the minimum at 248 K (see Eq. 2 and Fig. 5).

relaxation dynamics in the temperature range 200 K to 320 K. Our earlier measurements in the low- and high-frequency ranges (33, 36) lacked sufficient frequency coverage for testing the MCT scaling prediction, but the gap was bridged by the newly developed Nanosecond Acoustic Interferometry (NAI) method. The experimental methods and data analysis through which we determined the compliance spectra and the elastic modulus (the inverse of the compliance) are described in *SI Appendix*.

Fig. 2 presents the complex longitudinal modulus and compliance spectra of DC704 in the frequency range of $\sim 10^{-3}$ Hz to 10^{11} Hz. The imaginary parts of the spectra have gaps in the ranges of $\sim 10^4$ Hz to 10^6 Hz and 1 GHz to 10 GHz. To facilitate visualization of the temperature-dependent trends, the modulus and compliance spectra show only a subset of the data collected.

The primary temperature dependence, observed clearly in both real and imaginary components of the modulus spectra, is the movement of the alpha relaxation peak across about 9 decades to lower frequencies as the temperature is reduced toward the glass transition temperature $T_g \approx 210$ K. At any given frequency ω_0 , the real part of the modulus $M(\omega_0, T)$ increases as the sample is cooled, reflecting the stiffening of the liquid as it approaches the glassy state. At any given temperature T_0 , the real part of the modulus $M'(\omega, T_0)$ plateaus at frequencies above those of the alpha relaxation spectrum, because, at such high frequencies, the liquid cannot undergo structural relaxation during the acoustic oscillation period, resulting in a solid-like response.

The compliance spectra show analogous behavior upon cooling: movement of the alpha relaxation spectrum across many decades and a decrease in the real part at low temperatures and high frequencies. The beta relaxation feature is observed most clearly in the imaginary parts of the modulus and compliance functions, which both rise at high frequencies.

TTS

As examples of the use of broadband mechanical spectra, we have compared the data to the predictions of TTS (this section) and schematic MCT (next section, *Testing a Scaling Prediction of Schematic MCT*). TTS states that, for the alpha relaxation dynamics, the normalized density autocorrelation function can be written as $\Phi(t, T) = F[t/\tau_\alpha(T)]$. In other words, TTS states that a single temperature-independent functional form $F[t/\tau_\alpha(T)]$ describes the relaxation dynamics at all temperatures, with the temperature dependence contained only in the values of the characteristic relaxation time $\tau_\alpha(T)$. In that case, the alpha relaxation compliance loss spectrum $J''(\omega)$ has a temperature-independent shape in a log-log plot.

To test TTS, we normalized the imaginary compliance spectra by the peak heights and normalized the real spectra by the high-frequency limiting value J_∞ , and shifted both by amounts making the peak frequencies in $J''(\omega)$ coincide. The results are shown in Fig. 3. The alpha relaxation features superpose well across the entire temperature regime studied. The imaginary parts have the characteristic asymmetric shape found for most glass-forming materials: The low-frequency sides of the alpha relaxation spectra follow the Maxwell behavior, $J''(\omega) \propto \omega^1$, and the high-frequency sides follow a power law $J''(\omega) \propto \omega^{-1/2}$. The shifting of the spectra to make the alpha peaks overlap separates the beta relaxation features, which all appear at the high-frequency range in Fig. 2, on the scaled frequency axis. The scaled plots highlight the increase in separation between alpha and beta relaxations upon cooling.

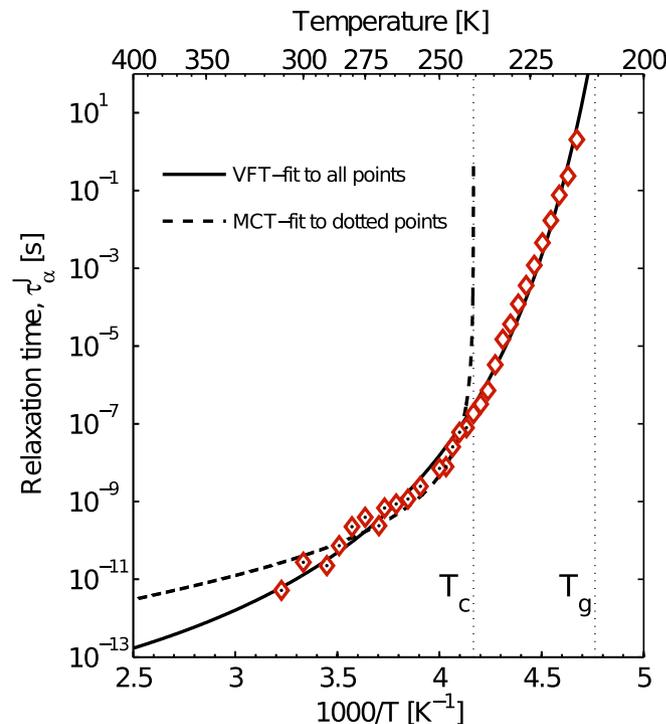


Fig. 4. The characteristic alpha relaxation time plotted as a function of inverse temperature where the Arrhenius equation gives a straight line. The glass transition temperature is $T_g \approx 210$ K. The VFT equation (see *Testing a Scaling Prediction of Schematic MCT*) was fitted to all data points (full line), yielding $\log \tau_0 = -15.0 \pm 0.8$, $D = 6 \pm 1$, and $T_0 = 183 \pm 5$ K. The MCT critical temperature $T_c = 240$ K was identified from Fig. 5C as the temperature below which MCT prediction breaks down; the MCT power law fit to the high-temperature points ($T > T_c$) (marked by central black dots) yielded the following fit parameters: $\log(\tau_\alpha/s) = -12.0 \pm 0.5$, $\gamma = 2.7 \pm 0.4$.

consistent with this prediction at temperatures above 240 K, but the relationship clearly breaks down below. We take this breakdown in the scaling relationship to define the critical temperature of schematic MCT, which is consistent with the fit of Fig. 4. Supporting this critical temperature assignment, the value of the alpha relaxation time at T_c , τ_α (240 K) ≈ 0.1 μ s, is typical for T_c , below which the schematic MCT breaks down (16) due to the onset of thermally assisted hopping (43–45) through which alpha relaxation continues to occur.

Fig. 5D compares the alpha relaxation critical exponent γ determined in Fig. 4 based on $T_c = 240$ K to the MCT prediction that connects the power-law exponents to γ through the relation (15)

$$\gamma = 1/(2a) + 1/(2b). \quad [4]$$

The above analysis indicates that schematic MCT applies at temperatures above 240 K for DC704. For the fits to be useful as a test of the MCT predictions, there must be sufficient separation between the alpha and beta relaxation spectra as $T \rightarrow T_c$ from above that the a and b exponents can be associated distinctly with the two features (26, 46). The separation was sufficient for our results below 248 K, and thus MCT can be meaningfully tested in the temperature range 240 K to 248 K.

Fig. 5A shows the region around the minima between the alpha and beta features of the compliance loss spectra $J''(\omega)$ at temperatures 240 K and 248 K. As a final test, Eq. 2 was compared with the data with fixed exponent values. Only the minimum frequency ω_{\min} and the minimum compliance loss J''_{\min} positions of each curve were adjusted to fit the data. The exponent value $b = 0.50$ was determined from the high-frequency wing of the alpha relaxation spectra evident in the TTS plot (Fig. 3). From this result, the predicted value of the exponent a could be calculated using Eq. 3; this yielded the value $a = 0.28$, which should describe the low-frequency wing of the beta relaxation spectra. The resulting prediction completely determines the shape of the curves that go through the data well within the experimental scatter.

Conclusions

Our measurements demonstrate the feasibility of obtaining broadband mechanical relaxation spectra of a glass-forming liquid reaching the high frequencies of the beta relaxation spectrum and extending to the low frequencies of the alpha relaxation spectrum even as T_g is approached. The results give direct experimental support for TTS of the alpha relaxation spectrum, both above and below the critical temperature of schematic MCT (240 K), the validity of which is often assumed in empirical studies of glass-forming liquids and in modeling used for practical applications. Our results also permitted calculation of the dynamic critical exponents of schematic MCT above T_c , yielding results consistent with predictions that relate the alpha and beta relaxation dynamics. We also have measured shear relaxation dynamics across a wide frequency range (36), and filling in the frequency gaps for these measurements will permit comparison between longitudinal and shear dynamics that may show distinct temperature-dependent behavior (47).

DC704 is the first sample for which mechanical relaxation dynamics have been measured across the frequency range we have explored. Additional glass-forming liquids must be examined to assess the generality of TTS and MCT predictions. Our results demonstrate that access is now available to the extraordinarily wide frequency range needed for such comprehensive tests of supercooled liquids and a wide range of partially disordered materials including relaxor ferroelectrics, block copolymers, and many others. We hope the techniques are developed further in the future to make such measurements faster and less demanding. If and when this happens, it is realistic to imagine

that broadband mechanical spectra will become as widely available as dielectric spectra are today.

Materials and Methods

Overview. The seven different measurement methods and the frequency ranges that they cover are summarized in Fig. 6; detailed descriptions of the techniques and data collected from them are discussed in *SI Appendix*. The techniques include three low-frequency methods involving piezoceramics that shear or compress the entire sample quasi-statically (33–35, 48) and four higher-frequency methods using short laser pulses to excite and subsequently detect acoustic waves in an irradiated region (30–32, 49–52).

The two lowest-frequency methods determine the complex frequency-dependent bulk modulus $K(\omega)$ and shear modulus $G(\omega)$ directly, where ω is the angular frequency. The longitudinal modulus is then given by $M(\omega) = M'(\omega) + iM''(\omega) = K(\omega) + (4/3)G(\omega)$. The four methods covering megahertz to gigahertz frequencies determine acoustic parameters. The complex longitudinal modulus is given from the acoustic data as $M(\omega, T) = \rho(T)(c_l(\omega, T))^2$, where $\rho(T)$ is the temperature-dependent density and $c_l(\omega, T)$ is the complex frequency-dependent longitudinal sound velocity.

To determine the modulus as a function of temperature from the sound velocity and damping rate, the thermal contraction of the sample must be accounted for. Using literature data of the thermal expansion coefficient $\alpha = 7.2 \times 10^{-4} [\text{K}^{-1}]$ (53, 54) and assuming this quantity is temperature-independent, the following expression for the temperature dependence of the density can be derived (36):

$$\rho(T) = \frac{\rho(T_{\text{ref}})}{1 + \alpha\rho(T - T_{\text{ref}})} = \frac{1.07[\text{kg/m}^3]}{1 + 7.2 \times 10^{-4}[\text{K}^{-1}](T - 298[\text{K}])}. \quad [5]$$

Once the modulus is obtained, the complex longitudinal compliance is given by $J(\omega) = 1/M(\omega) = J'(\omega) - iJ''(\omega)$.

MCT relations are predictions for the mechanical susceptibility $\chi(\omega)$ to which $J(\omega)$ is proportional. Strictly speaking, $\chi(\omega)$ is related to the density autocorrelation function and therefore to the bulk compliance, not the longitudinal compliance. However, the difference between $K(\omega)$ and $M(\omega)$ (and thus also the bulk and longitudinal compliances) is very small because the shear modulus is considerably smaller than the longitudinal modulus, and their frequency-dependent dynamics are similar at both low (33, 55, 56) and high (47) frequencies.

Sample Preparation. For the PSG, PBG, and ISS measurements, DC704 was obtained from Sigma-Aldrich and used without purification. For the ISS measurements, the liquid was transferred into the cell through a 0.22- μ m millipore filter into a fused quartz cuvette. During the ISS measurements, the sample was observed to become slightly opaque at the coldest temperatures; this is likely due to phase separation of dissolved impurities from the base liquid, and it disappeared when the liquid was reheated. The problem was overcome in subsequent experiments by mixing the sample with anhydrous MgSO_4 , combined with heating under vacuum before filtration. This approach was adopted for the NAI, TDBS, and PUI techniques. Comparison of data both with and without treatment by the drying agent showed no difference in the acoustic parameters. The DC704 samples never crystallized during the course of our experiments.

The transducer techniques use home-built closed-cycle cryostats capable of keeping the temperature constant within a few millikelvins (57), and the NAI and ISS measurements were performed in a commercially available cold-finger cryostat. In these measurements, temperature sensing was provided by factory-calibrated platinum resistors immersed in the liquid a few millimeters away from the optical beams. The TDBS and PUI techniques were performed in a commercial sample-in-vapor cryostat, and the temperature was monitored at a position a few millimeters away from the sample.

We did not carry out any calibration of temperatures between the cryostats of the different laboratories. However, the low-frequency part of the longitudinal spectrum was obtained as the sum of two individual measurements that were carried out in the same experimental setup (same cryostat, same electronics). We estimate that the uncertainty on the absolute temperature is less than the overall noise in the high-frequency methods.

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